



# Chiral Wobbling in $^{135}\text{Pr}$

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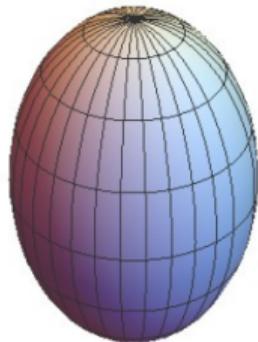
Fall Meeting of the Division of Nuclear Physics of the American Physical Society

October 16, 2019

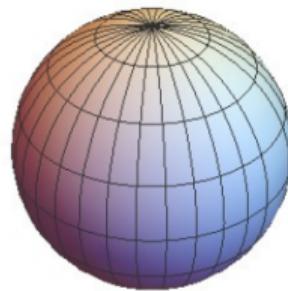
University of Notre Dame

# Nuclear Shapes

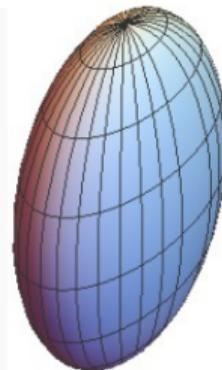
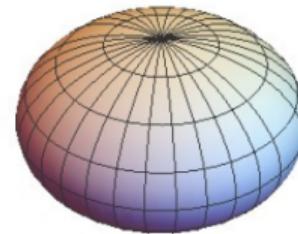
Prolate



Spherical



Oblate

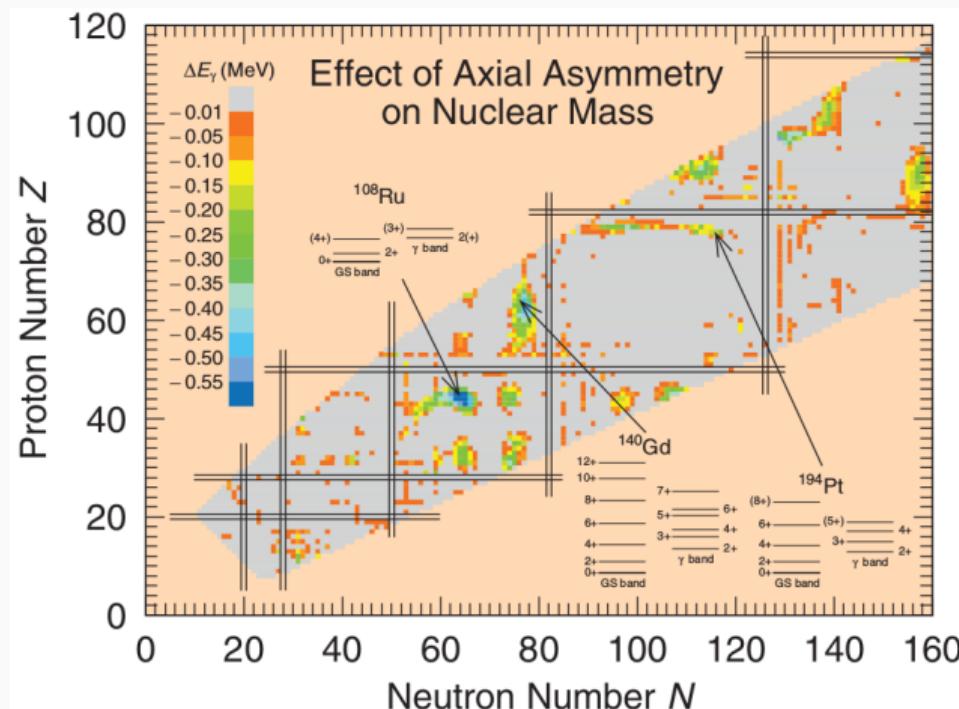


Triaxial

# Triaxial Region

Triaxiality - A rare phenomenon!

P. Möller et. al. PRL 97, 162502 (2006)

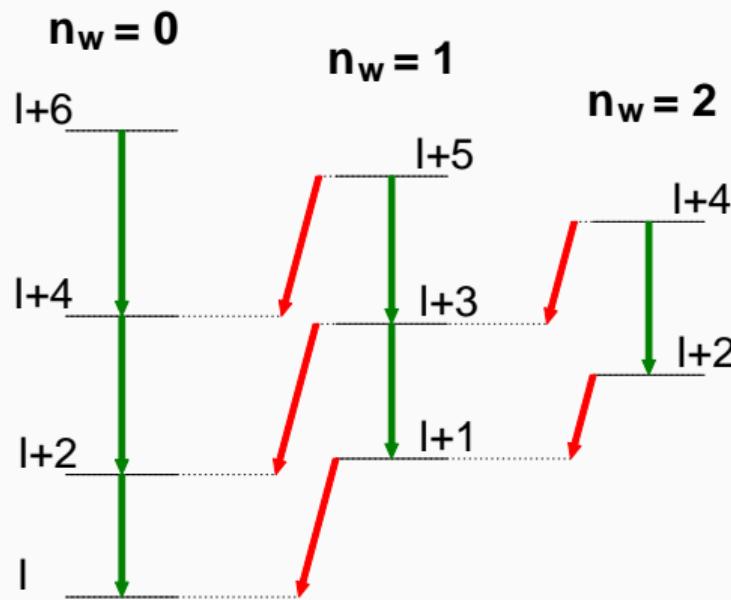


## Wobbling - Unique fingerprint of Triaxiality (1/2)

- Harmonic oscillation of one of the principal axes about the space fixed  $\vec{J}$ .
- Analog of the spinning motion of an asymmetric top.
- For odd-A nuclei:
  - Odd particle aligns with m-axis - Longitudinal wobbling
  - Odd particle aligns  $\perp$  to m-axis - Transverse wobbling

Animation courtesy - J. T. Matta

## Wobbling - Unique fingerprint of Triaxiality (1/2)



**Standard fingerprints for Wobbling bands:**

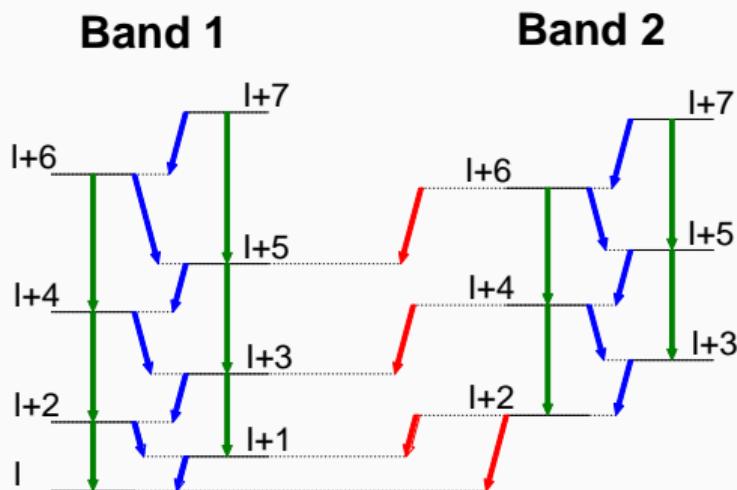
- Rotational bands corresponding to  $n_w = 0, 1, 2, \dots$
- Transitions from  $n_{w+1} \rightarrow n_w$  ( $\Delta n_w = +1$ )
- Interband Transitions are  $\Delta I = 1$ , E2

## Chirality - Unique fingerprint of Triaxiality (2/2)

Animation courtesy - X. H. Wu

- Axis of rotation lies outside all of the three principal planes of the nucleus.
- High- $j$  particles align with the s-axis, high- $j$  holes align with the l-axis and the triaxial core rotates about the m-axis.
- This arrangement breaks the time-reversal symmetry.
- The system is R.H. if the s-, m- and l-axes are ordered counterclockwise w.r.t  $\vec{J}$  and L.H. otherwise.

## Chirality - Unique fingerprint of Triaxiality (2/2)

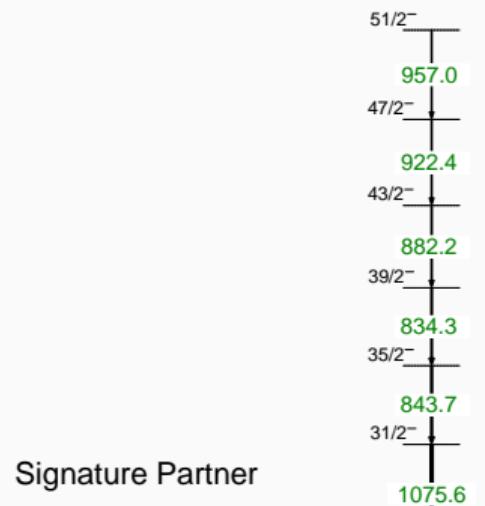


### Standard fingerprints for Chiral bands:

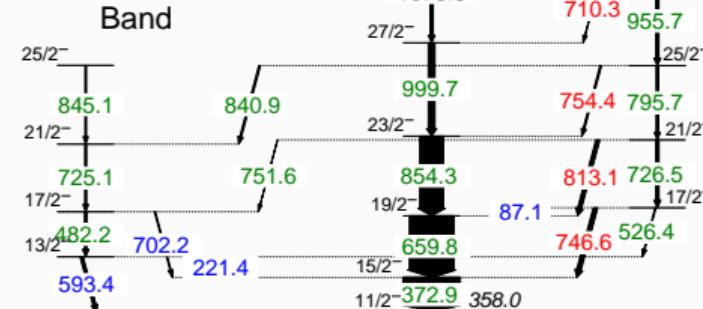
- Opposite chirality bands - Two  $\Delta I = 1$  bands of same parity
- Close excitation energies
- Constant staggering parameter
- Identical  $B(M1)/B(E2)$  ratios

# Level Scheme of $^{135}\text{Pr}$

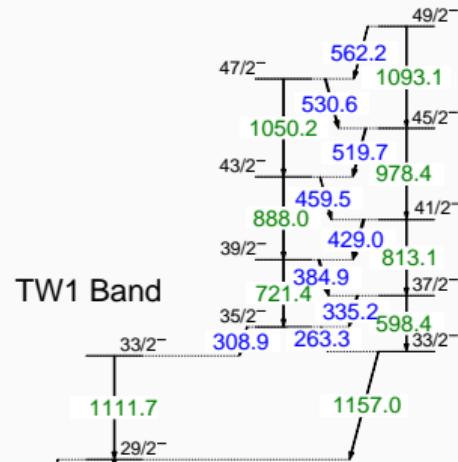
**What we know so far ...** Yrast Band



Signature Partner

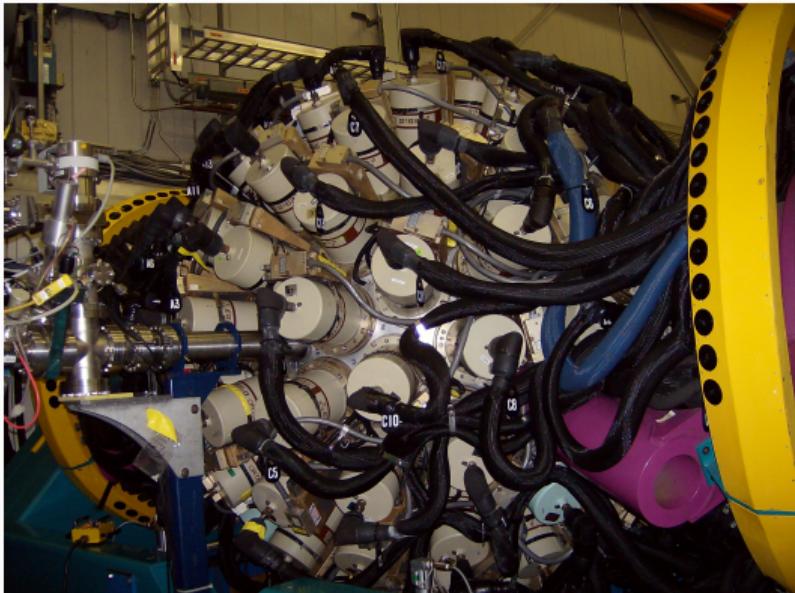


Dipole Band



J. T Matta et al., PRL 114,  
082501 (2015)

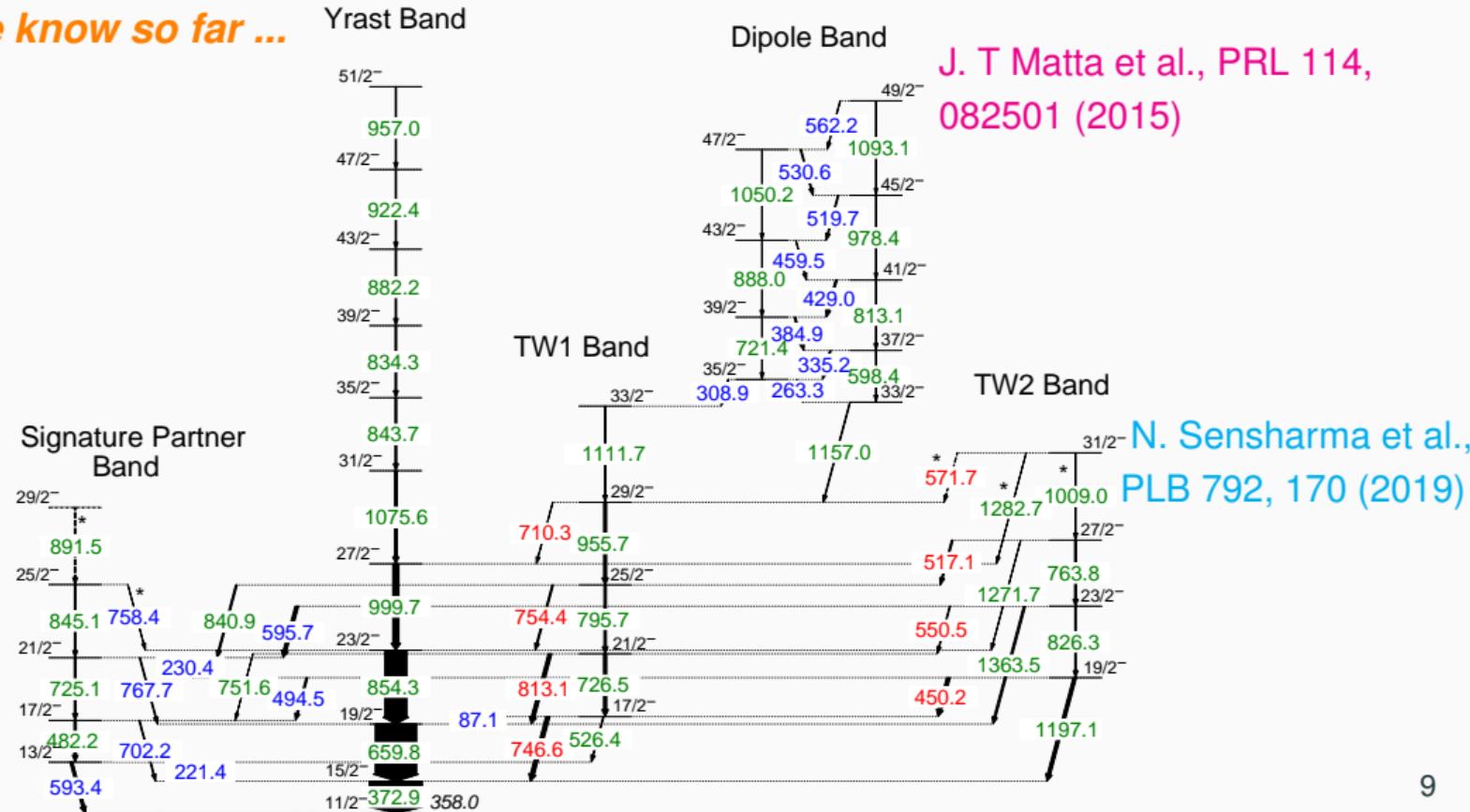
## Experimental Details (1/2)



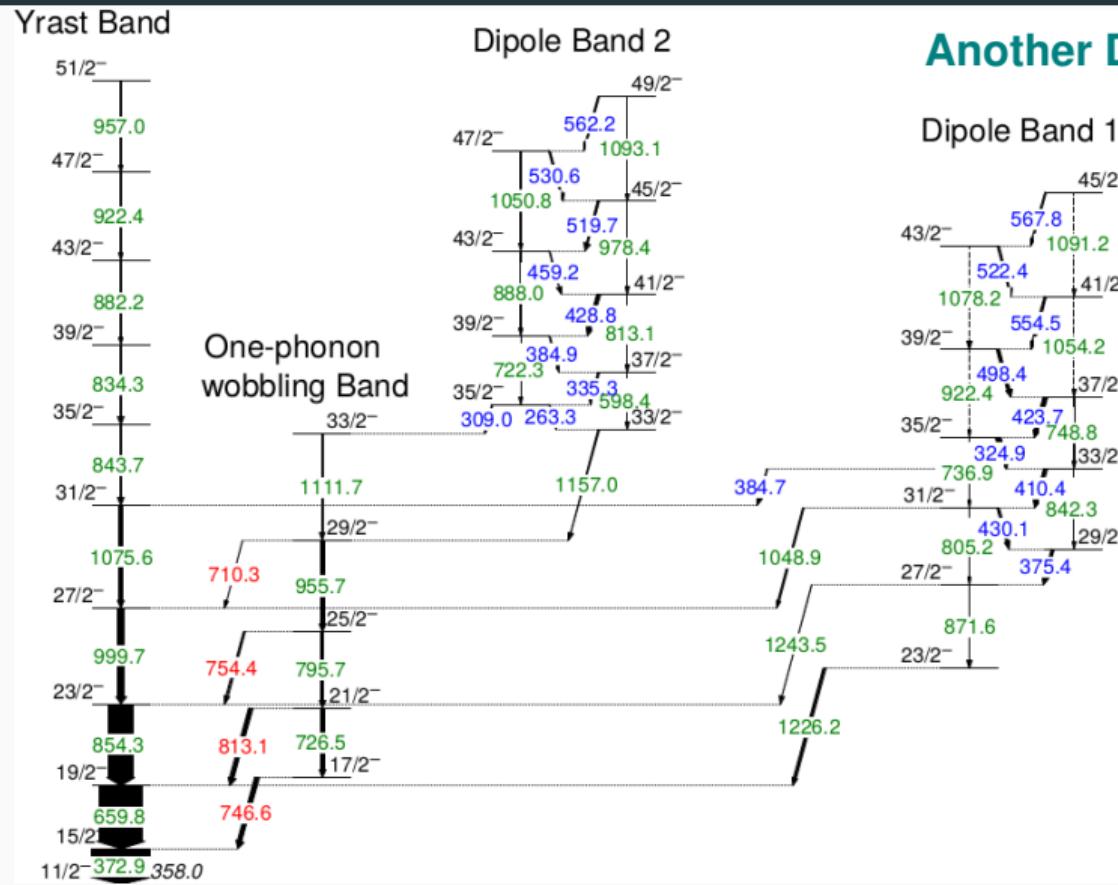
- Experiment performed using the Gammasphere facility at Argonne National Laboratory.
- Reaction used:  $^{123}\text{Sb}(^{16}\text{O},4\text{n})^{135}\text{Pr}$  at 80 MeV.
- 83 compton suppressed HpGe detectors used.
- No. of three- and higher-fold  $\gamma$ -ray coincidence events  $\approx 1.5 \times 10^{10}$ .

# Level Scheme of $^{135}\text{Pr}$ (cont.)

**What we know so far ...**



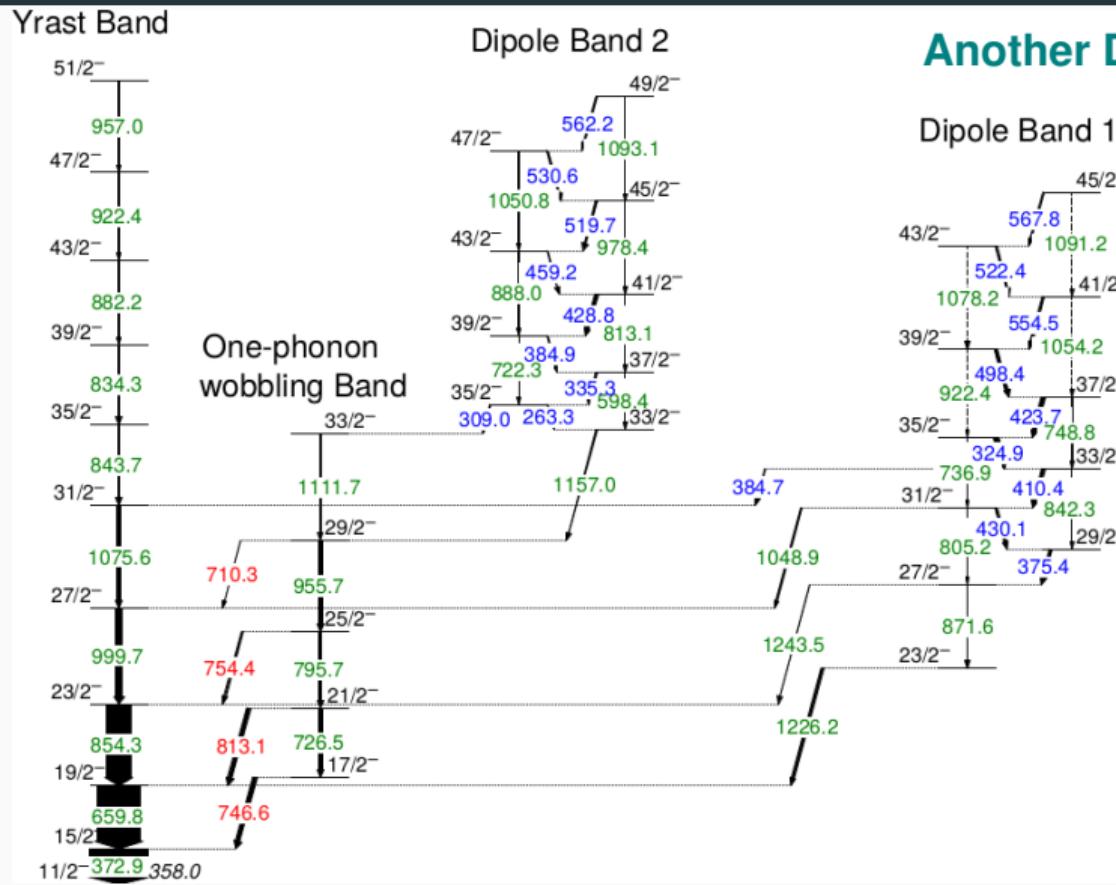
## Level Scheme of $^{135}\text{Pr}$ (cont.)



## Another Dipole Band

## Dipole Band 1

# Level Scheme of $^{135}\text{Pr}$ (cont.)

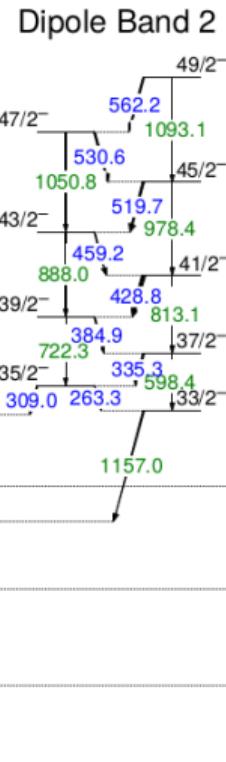
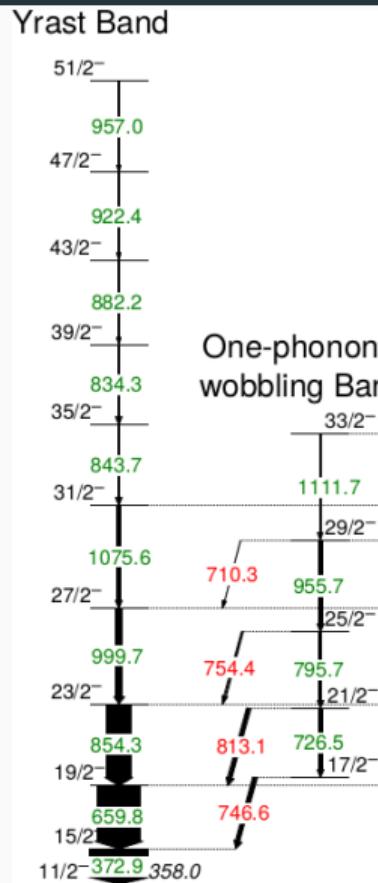


Another Dipole Band

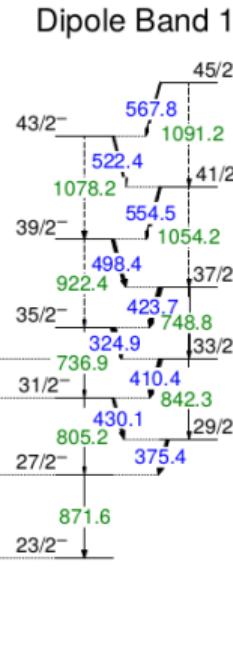
Dipole Band 1

Origin?

# Level Scheme of $^{135}\text{Pr}$ (cont.)



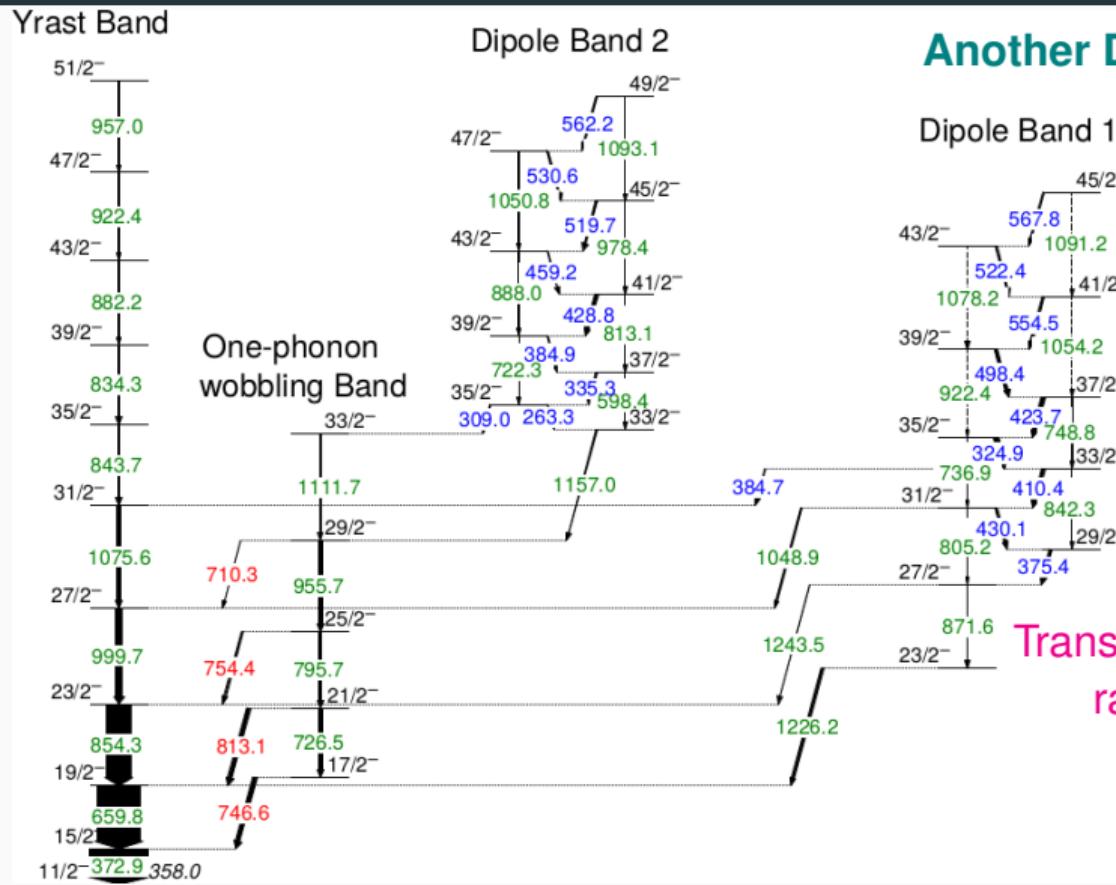
**Another Dipole Band**



Origin?

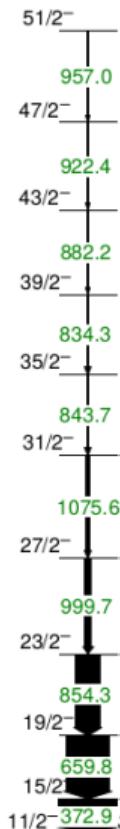
Any linking transitions?

# Level Scheme of $^{135}\text{Pr}$ (cont.)

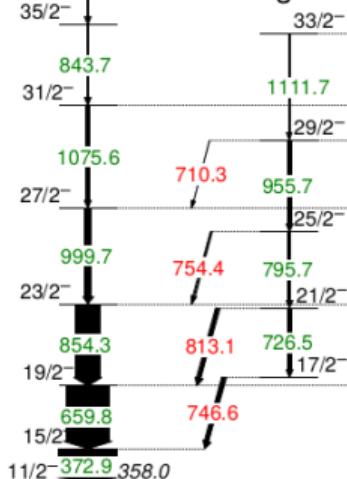


# Level Scheme of $^{135}\text{Pr}$ (cont.)

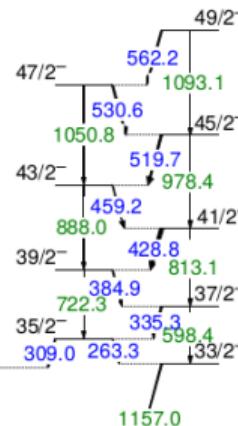
Yrast Band



One-phonon wobbling Band

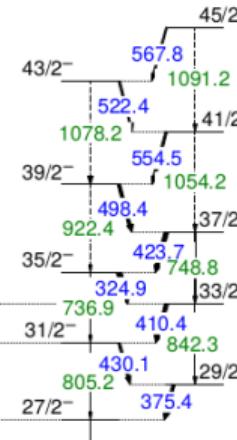


Dipole Band 2



Another Dipole Band

Dipole Band 1



Origin?

Any linking transitions?

Transition probability ratios?

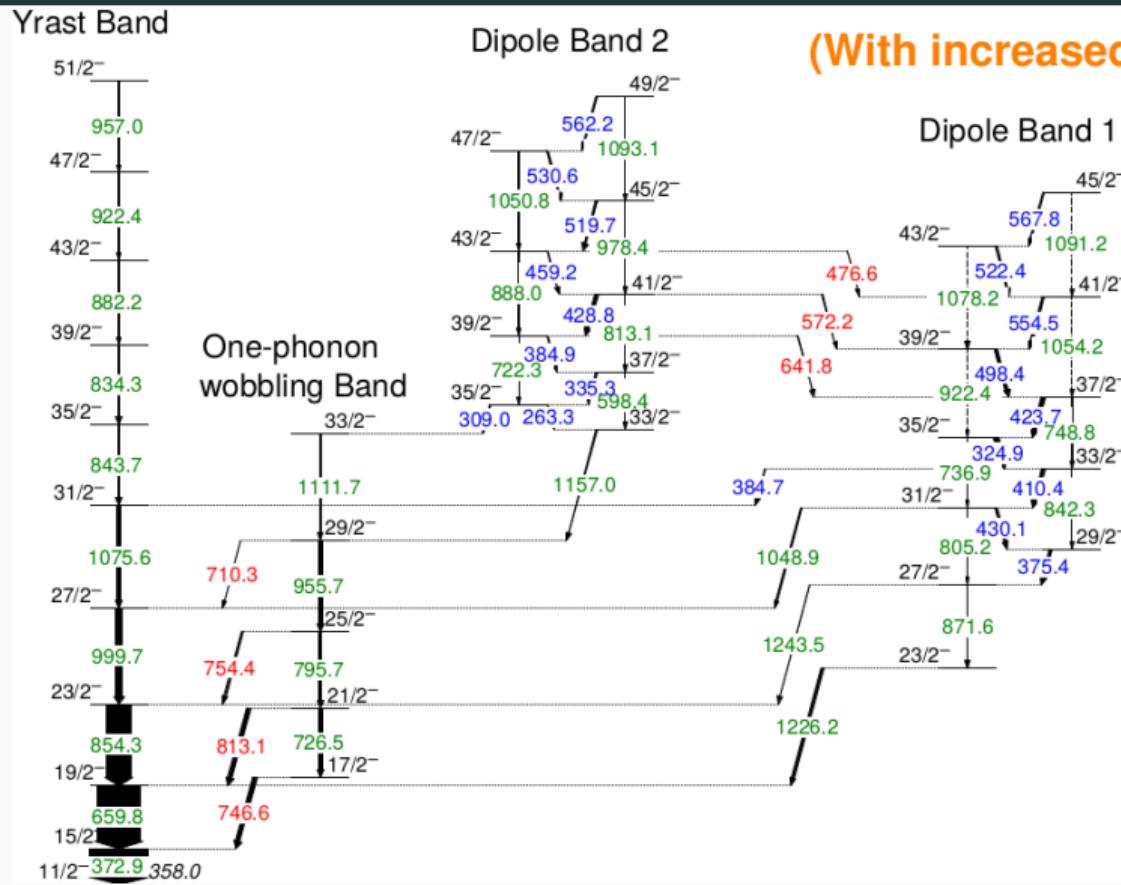
Insufficient statistics

## Experimental Details (2/2)

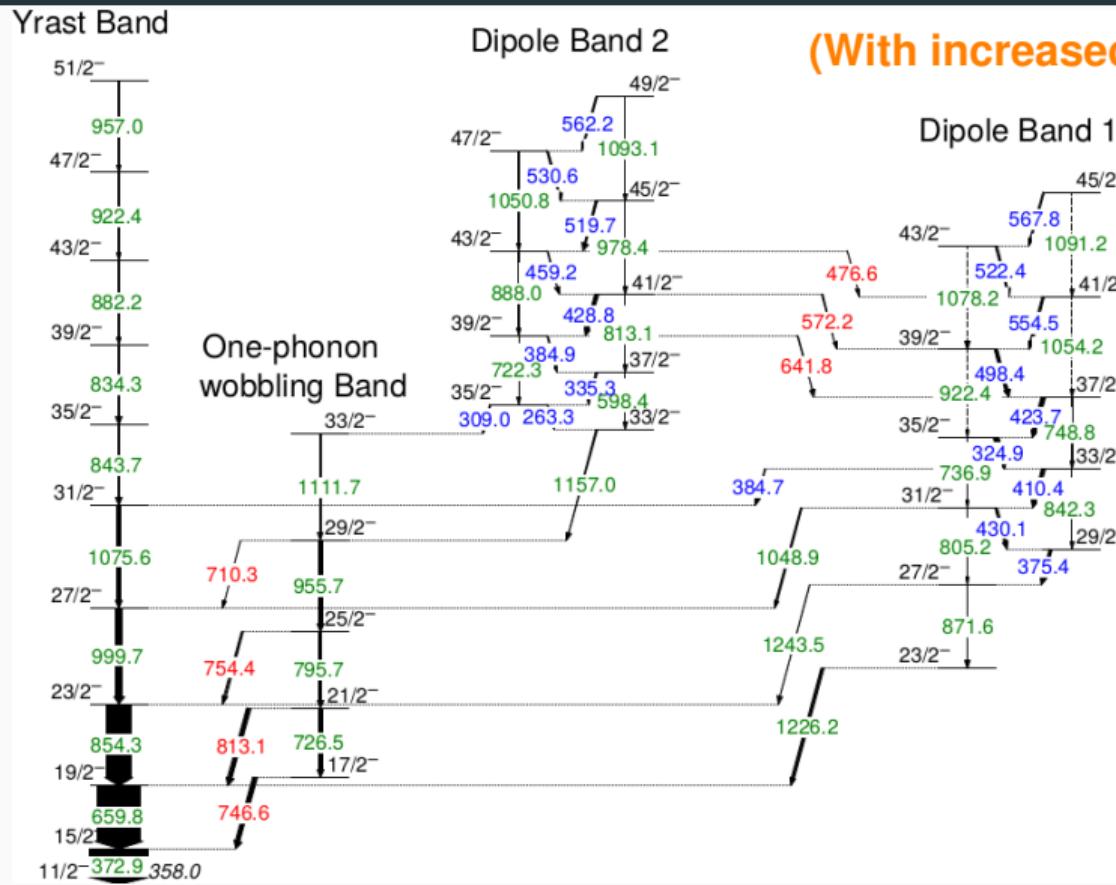


- Experiment repeated using the Gammasphere facility at Argonne National Laboratory.
- Same reaction, energy and similar targets as previous experiment.
- 63 compton suppressed HpGe detectors used.
- Both datasets added together.
- Total no. of three- and higher-fold  $\gamma$ -ray coincidence events  $\approx 2.5 \times 10^{10}$ .

# Level Scheme of $^{135}\text{Pr}$ (cont.)

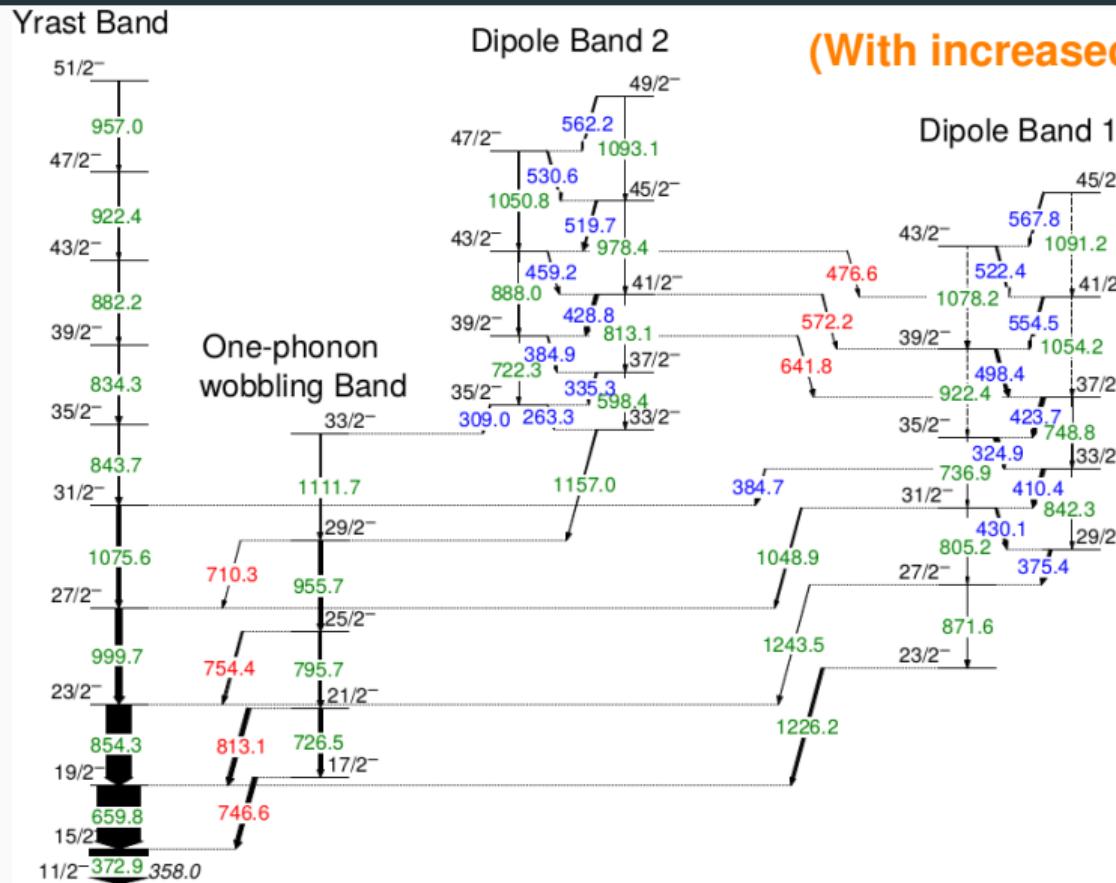


# Level Scheme of $^{135}\text{Pr}$ (cont.)



Three linking transitions

# Level Scheme of $^{135}\text{Pr}$ (cont.)

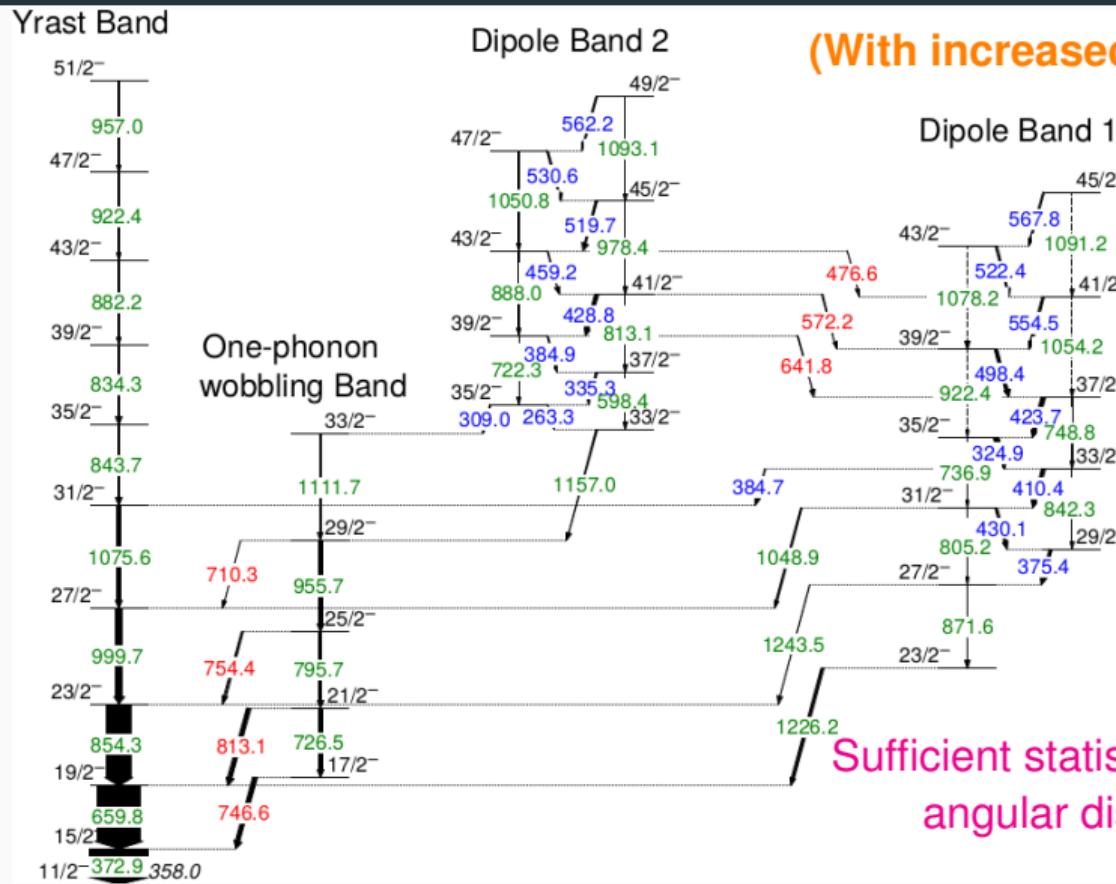


(With increased statistics)

Three linking transitions

Could these be  
Chiral  
Partners??

## Level Scheme of $^{135}\text{Pr}$ (cont.)



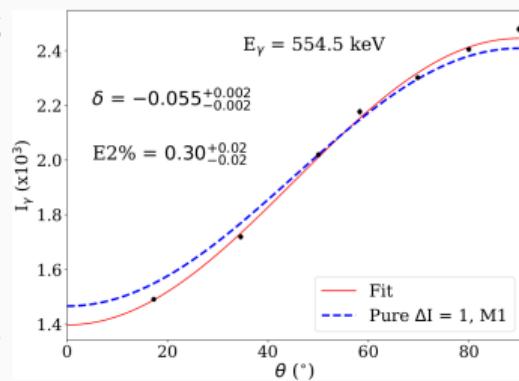
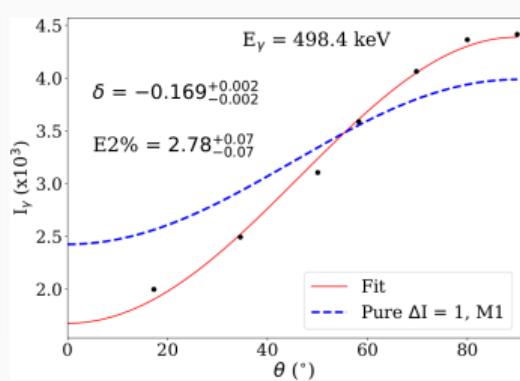
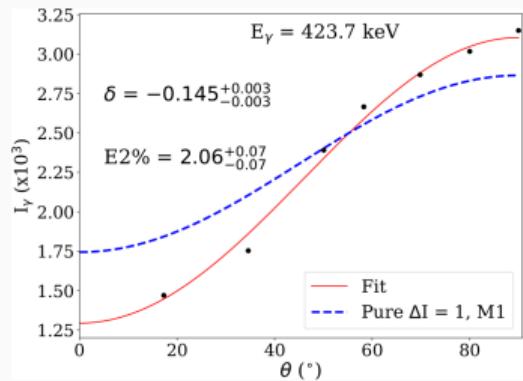
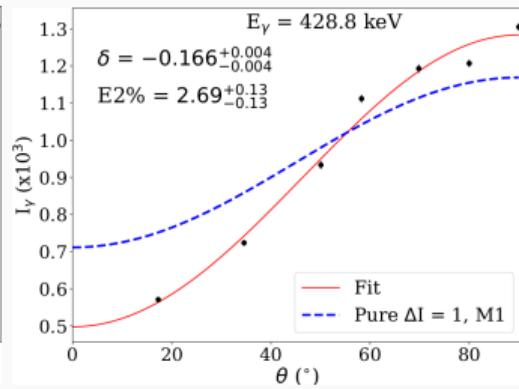
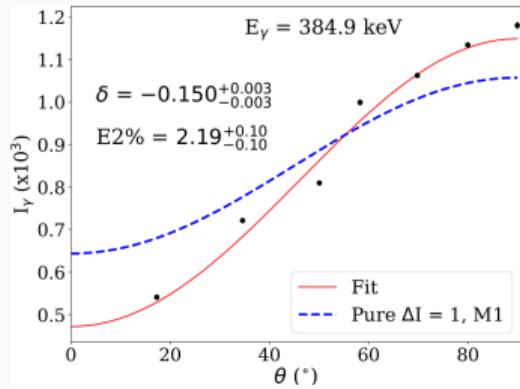
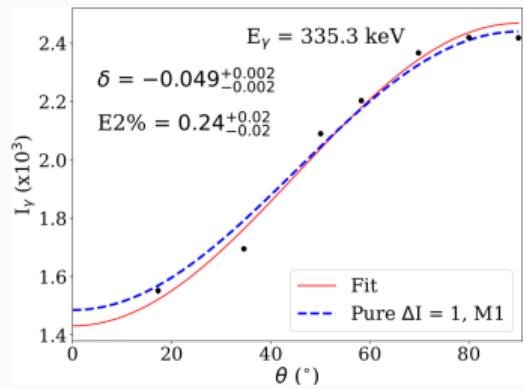
**(With increased statistics)**

## <sup>2-</sup> Three linking transitions

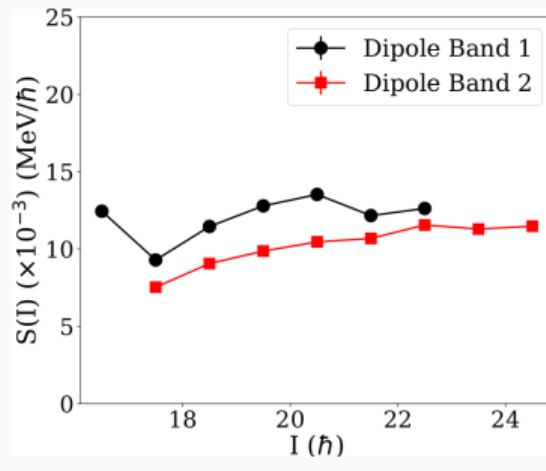
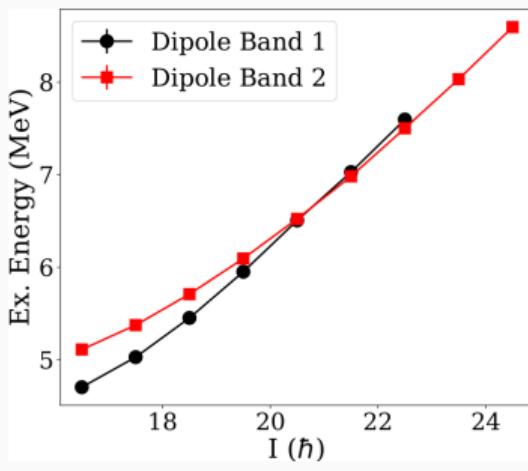
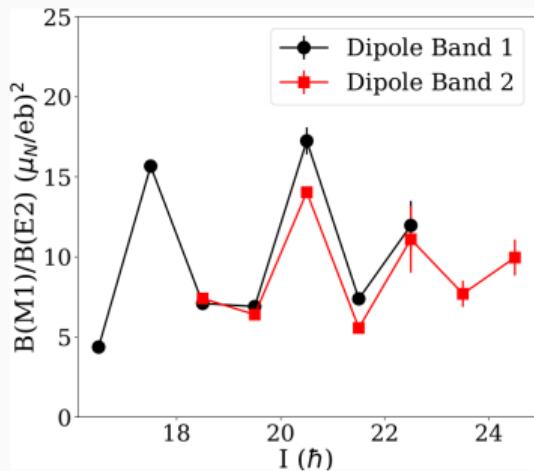
- Could these be Chiral Partners??

## Sufficient statistics to perform angular distributions

# Angular Distributions (1/4)



## Other parameters



Reduced transition  
Probability ratios

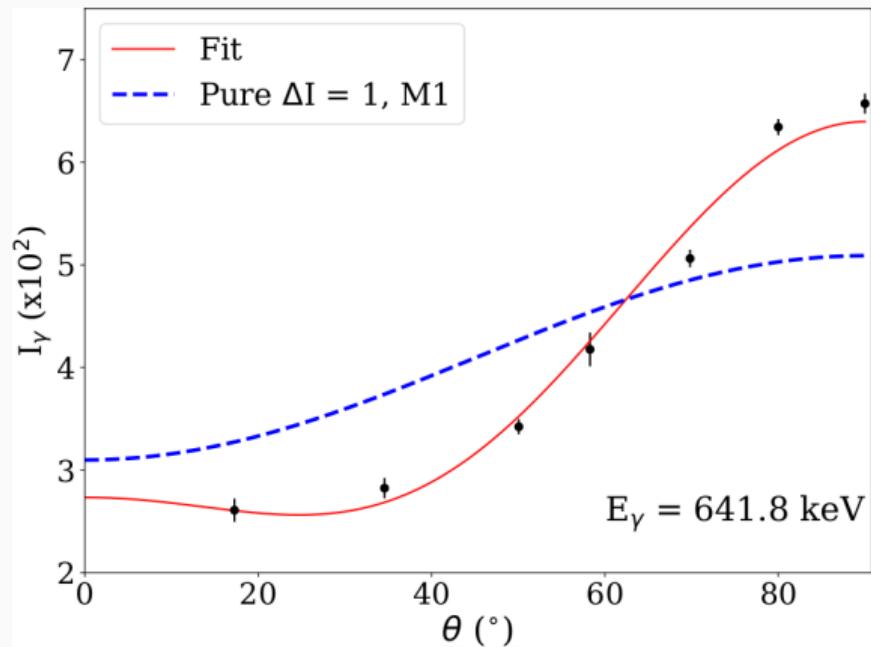
Excitation Energy

Staggering Parameter

## Angular Distributions (2/4)

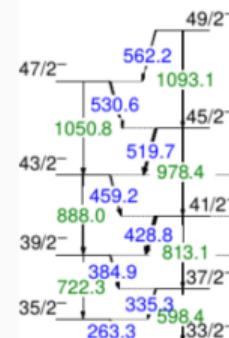
$$E_\gamma = 641.8 \text{ keV}$$

$$\delta = -2.92^{+0.12}_{-0.13}$$

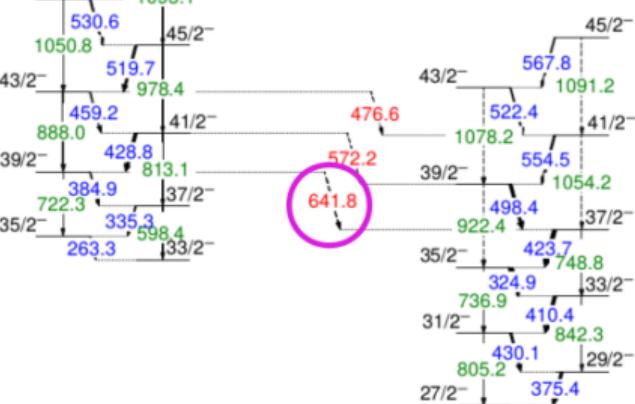


$$E2\% = 89.5^{+0.8}_{-0.8}$$

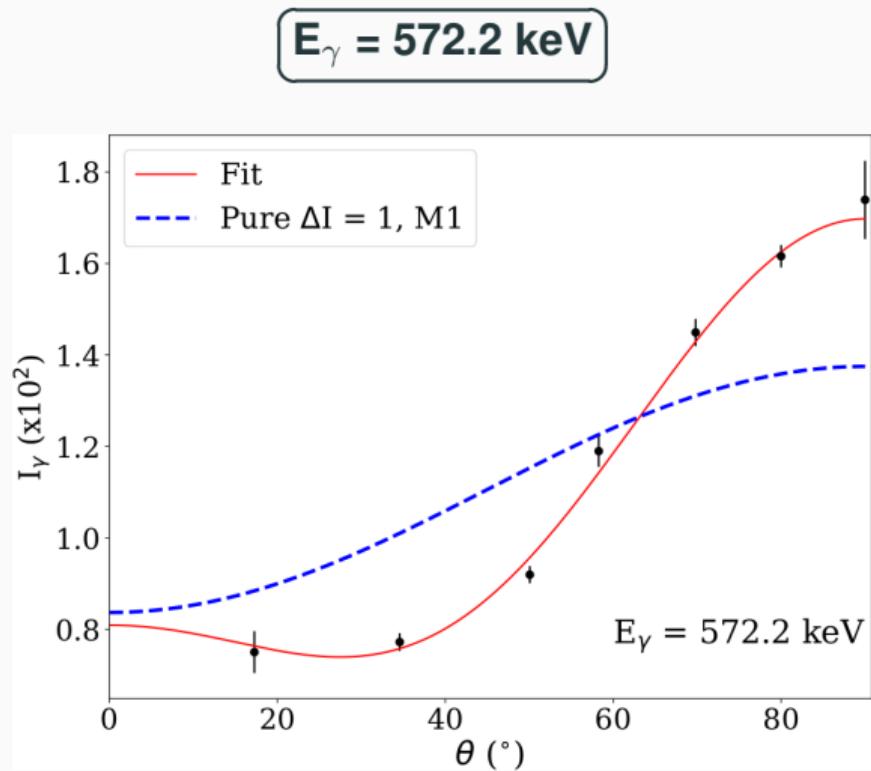
Dipole Band 2



Dipole Band 1



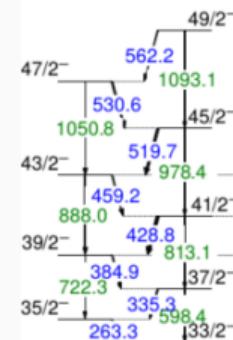
## Angular Distributions (3/4)



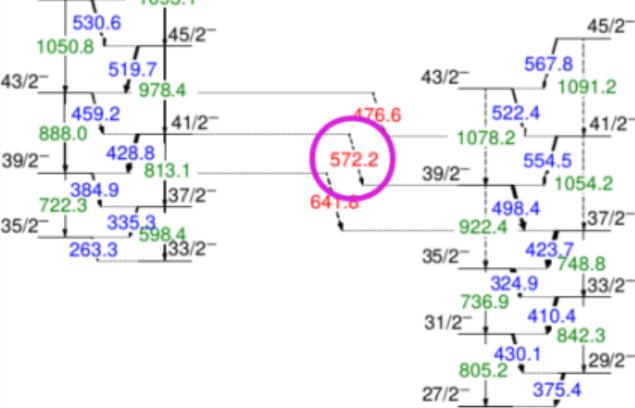
$$\delta = -3.31^{+0.16}_{-0.18}$$

$$E2\% = 91.6^{+0.8}_{-0.8}$$

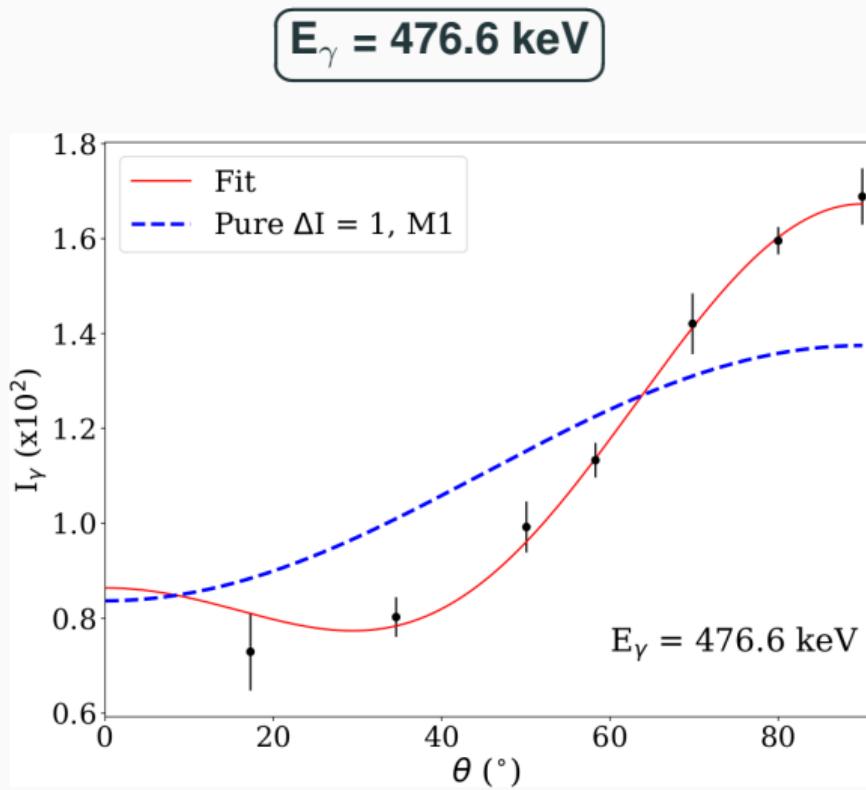
Dipole Band 2



Dipole Band 1

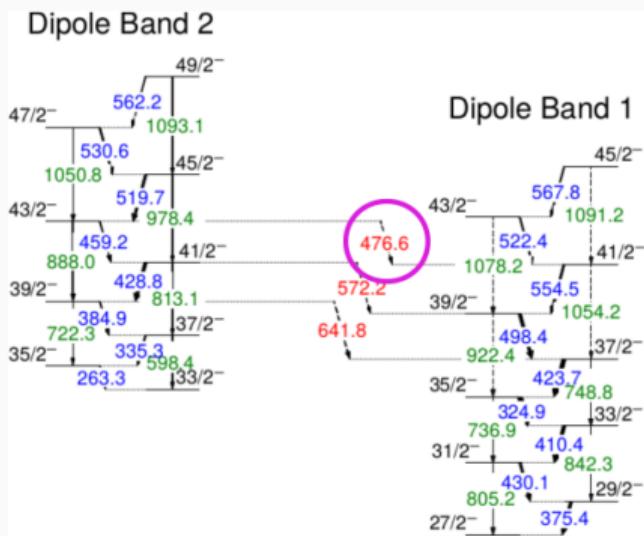


## Angular Distributions (4/4)

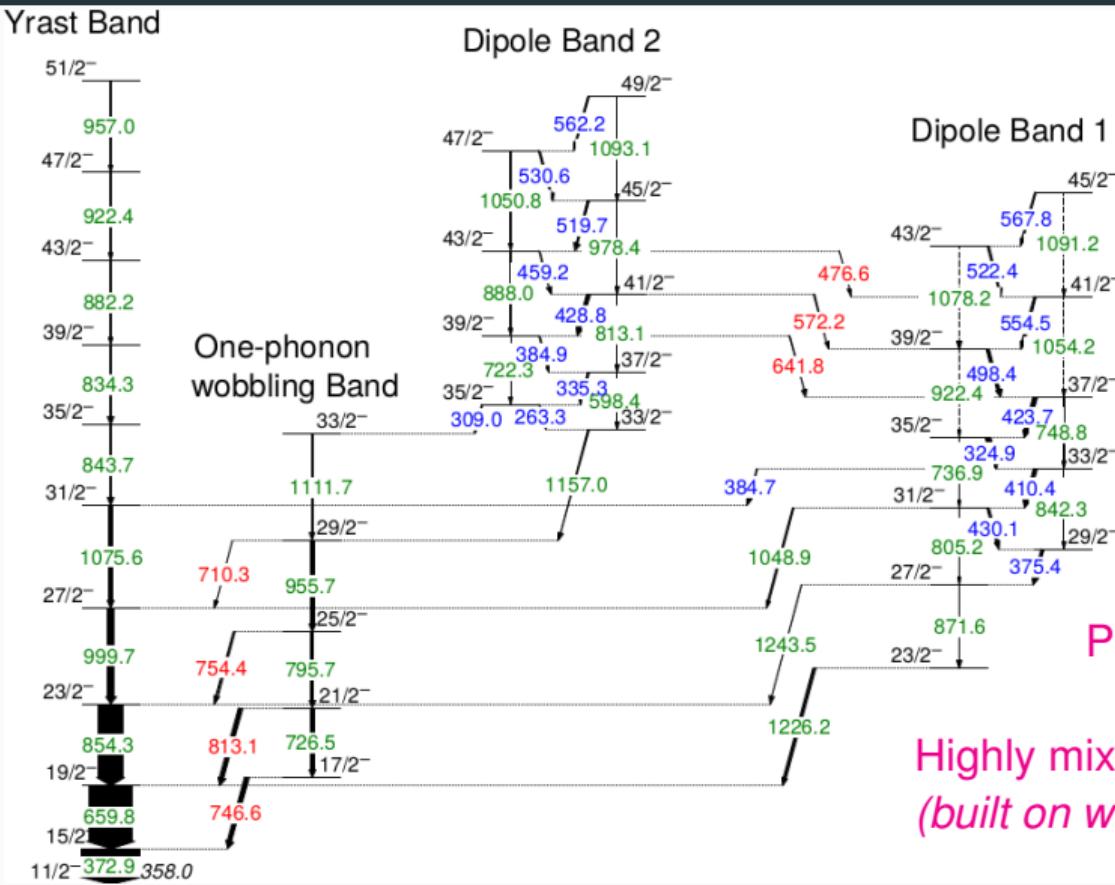


$$\delta = -3.68^{+0.34}_{-0.39}$$

$$E2\% = 93.1^{+1.2}_{-1.3}$$



# Level Scheme of $^{135}\text{Pr}$ (cont.)



Two  $\Delta I = 1$  bands

Same parity

Similar energies

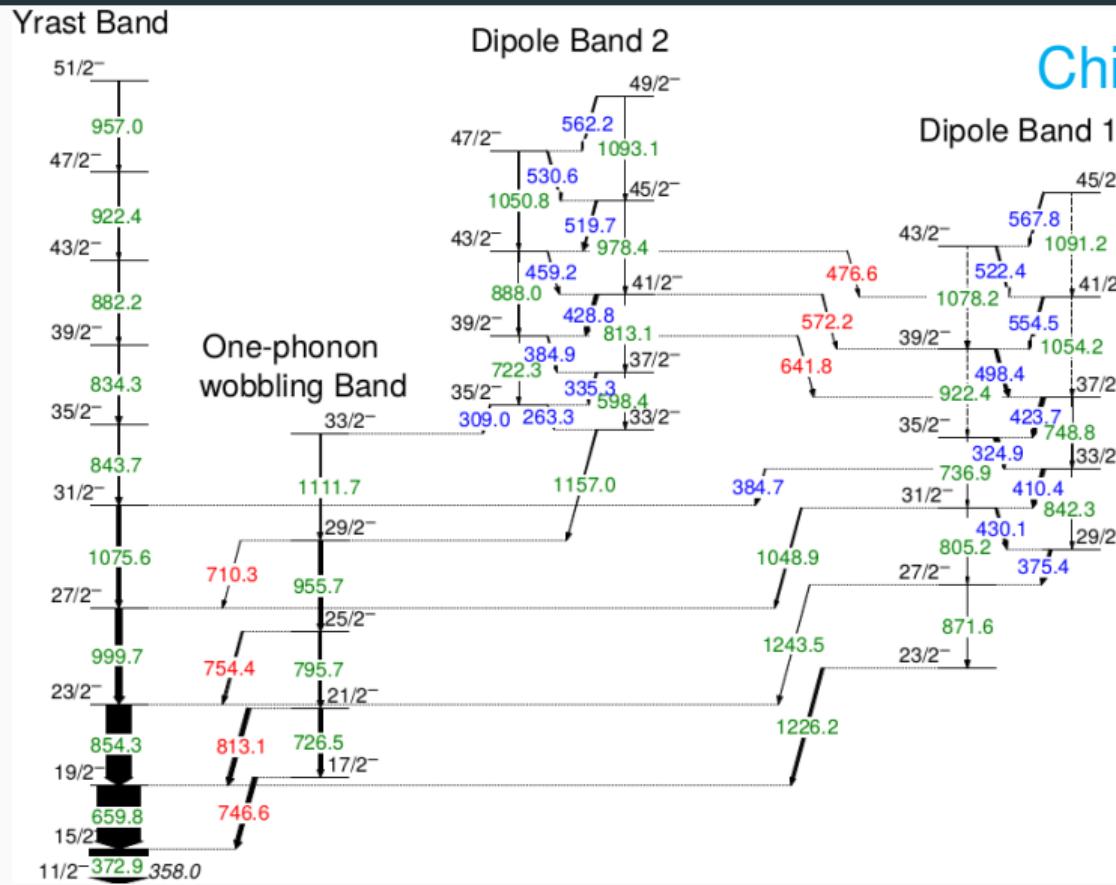
Nearly constant staggering

Identical  $B(M1)/B(E2)$  ratios

Pure M1 in-band transitions

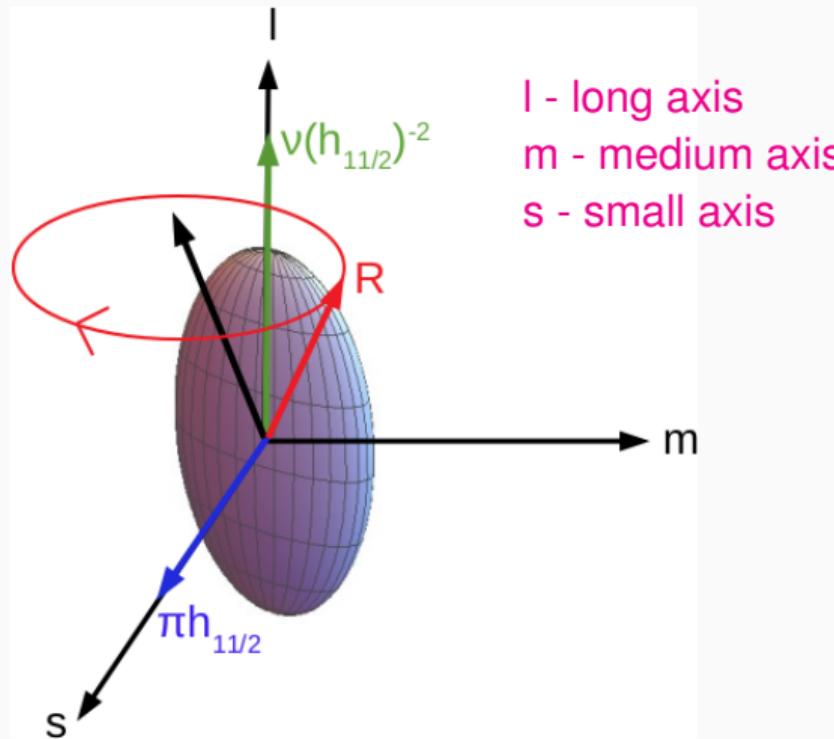
Highly mixed M1+E2 linking transitions  
(built on wobbling excitations)

# Level Scheme of $^{135}\text{Pr}$ (cont.)



Chiral Partners!

# Chiral Wobbling in $^{135}\text{Pr}$

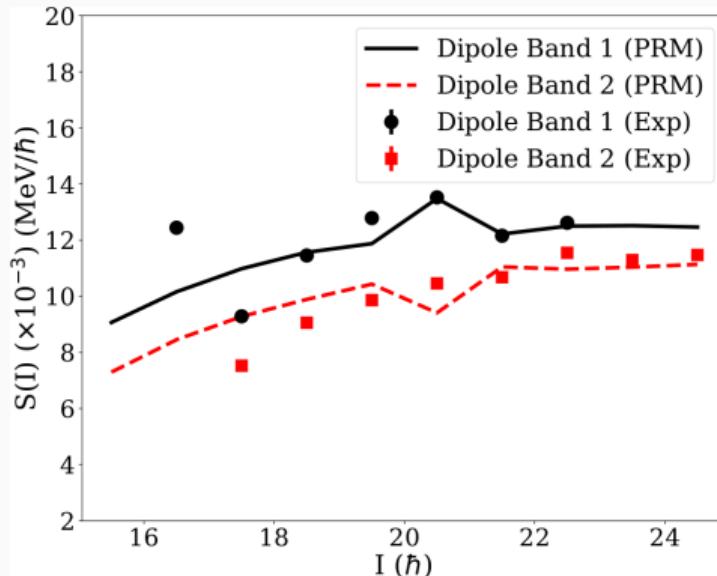
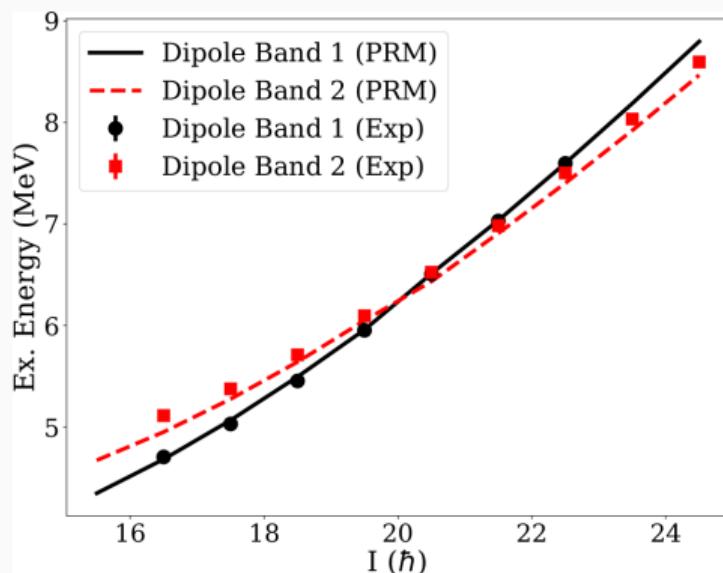


- Two additional  $h_{11/2}$  neutron holes align along the *I*-axis.
- Net angular momentum generated in the *s*-*I* plane.
- Collective  $\vec{R}$  precesses along this axis.
- Collective excitation of the wobbling type.

# Signatures of Chirality

## Preliminary theoretical results

- Close excitation energies
- Constant staggering parameter



## Conclusion and Future Work

- The phenomenon of chiral wobbling motion has been investigated in  $^{135}\text{Pr}$ .
- $^{135}\text{Pr}$  - first possible case of *Chiral wobbling*.
- High statistics angular distribution measurements performed.
- Ongoing analysis to extend the two dipole bands and find more connecting transitions.
- Calculations in the framework of the Particle Rotor Model (PRM) being done to affirm experimental observations.

# Acknowledgements

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